

## Unlocking Precision: A Comprehensive Guide to Approximation

# Introduction:

We use approximation in our daily life every day, we all know how to do it, for example we say 1000 for 999, what we do we simply ignore a comparably small portion.

In mathematical expressions which include division and multiplication of decimal values of large numbers we are stuck. It becomes quite complex to solve these problems, so for solving these we use approximation. We just Round-off the numbers.

When we approximate the final result obtained is not equal to the exact result, but it is very close to the exact result.

Let's try one,

**E.g.**  $? = 32.01 + 128.01 \times 1023.99 + 7.99$

Solving by **BODMAS** rule, as learned earlier

$$\Rightarrow ? = 32.01 + 128.01 \times 1023.99 + 7.99$$

$$\Rightarrow ? = 32.01 + 131,080.9599 + 7.99$$

$$\Rightarrow ? = 32.01 + 131,080.9599 + 7.99$$

$$\Rightarrow ? = 131,120.9599$$

**E.g.**  $10\% \text{ of } 1350 + ? = 365$

$$\Rightarrow 10/100 \times 1350 + ? = 365$$

$$\Rightarrow 135 + ? = 365$$

$$\Rightarrow ? = 365 - 135 \Rightarrow ? = 230$$

**E.g.**  $78 \times 98 - 25\% \text{ of } 1376$

$$\Rightarrow 78 \times 98 - 25/100 \times 1376$$

$$\Rightarrow 7644 - 34400/100$$

$$\Rightarrow 7644 - 344 = 7300 \text{ (it requires tedious calculation)}$$

After this tedious calculation ( $128.01 \times 1023.99$ ) without a calculator, we are not left with time, in the exam hall we will prefer to leave this question.

In Approximation, to solve the complex mathematical expression, take the nearest value of numbers given in the expression. Try to make unit digit 0' in most cases.



## Unlocking Precision: A Comprehensive Guide to Approximation

**E.g.**  $? = 32.01 + 128.01 \times 1023.99 + 7.99$

Let's try to round off to nearest integer

$$\Rightarrow ? = 32 + 128 \times 1024 + 8$$

Or we can say,

$$\Rightarrow ? = 2^5 + 2^7 \times 2^{10} + 2^3$$

$$\Rightarrow ? = 2^5 + 2^{17} + 2^3$$

$$\Rightarrow ? = 2^3 (2^2 + 2^{14} + 1)$$

$$\Rightarrow ? = 8 (16389) = 131112$$

By calculator we would get 131112.09

Here it is, we got the solution.

**E.g.**  $393 \times 197 + 5600 \times 5/4 + 8211.80 = ?$

$$\Rightarrow 393 \times 197 + 5600 \times 5/4 + 8211.80 = ?$$

$$\Rightarrow 390 \times 200 + 5600 \times 5/4 + 8200 = ?$$

$$\Rightarrow 390 \times 200 + 5600 \times 5/4 + 8200 = ?$$

(By BODMAS rule)

$$\Rightarrow 390 \times 200 + 7000 + 8200 = ?$$

$$\Rightarrow 78000 + 7000 + 8200 = ?$$

$$\Rightarrow ? = 93200 \text{ (Ans).}$$

We got 92,632.8 by calculator. It is quite near its original value.

**Tip-** For finding 10% of a number simply move the decimal to one digit left.

For finding 25% simply divides the number by 4

**Shortcut method for Percentage:**

## Unlocking Precision: A Comprehensive Guide to Approximation

Sr. No.	Required Percentage (%)	Number divided by
1.	200	1/2
2.	50	2
3.	33.33	3
4.	25	4
5.	20	5
6.	10	10
7.	5	20
8.	1	100

**E.g.**  $10\% \text{ of } 1350 + ? = 365$

$\Rightarrow ? = 365 - 10\% \text{ of } 1350$

$\Rightarrow ? = 365 - 135.0$

$\Rightarrow ? = 230.0 \text{ (Ans).}$

**E.g.**  $78 \times 98 - 25\% \text{ of } 1376$

$\Rightarrow 78 \times 98 - 344 \text{ (Using approximation and table)}$

$\Rightarrow 8000 - 344$

$\Rightarrow 7656 \text{ (Ans).}$

This can be done in mind without the pen and paper.

**E.g.**  $34.02\% \text{ of } 550.09 + ? = 297.07 + \sqrt{728.95}$

$\Rightarrow 34.02\% \text{ of } 550.09 + ? = 297.07 + \sqrt{728.95}$

$\Rightarrow 34\% \text{ of } 550 + ? = 300 + \sqrt{729}$



## Unlocking Precision: A Comprehensive Guide to Approximation

$$\Rightarrow (25 + 10 - 1)\% \text{ of } 550 + ? = 300 + 27$$

$$\Rightarrow 25\% \text{ of } 550 + 10\% \text{ of } 550 - 1\% \text{ of } 550 + ? = 327$$

$$\Rightarrow 137.5 + 55 - 5.5 + ? = 327$$

$$\Rightarrow 132 + ? = 327$$

$$\Rightarrow ? = 327 - 132$$

$$\Rightarrow ? = 195 \text{ (Ans).}$$

**E.g.**  $(? + 9.97) \times 12.8 = 20.12\% \text{ of } 1319.97$

$$\Rightarrow (? + 10.00) \times 13.0 = 20.00\% \text{ of } 1320.00$$

$$\Rightarrow (? + 10.00) \times 13.0 = \frac{1}{5} \times 1320.00$$

$$\Rightarrow (? + 10.00) \times 13.0 = 264$$

$$\Rightarrow (? + 10.00) = 260/13$$

$$\Rightarrow ? = 20 - 10$$

$$\Rightarrow ? = 10 \text{ (Ans)}$$

So this is all for today. Try the questions of this topic. In the next blog, we will discuss some other topics.